

## Course Review

# Chapter 11 - Sequences and Series

## 11-1 Sequences and Series

**Sequence:** A function whose domain is the set of positive integers (1, 2, 3, ...) called "terms" and the listing of output values that follow some function rule.

EXAMPLE:  $a_n = 3(n-2)$ ; terms: 1, 2, 3; sequence: -3, 0, 3;

- finite sequence: domain is finite
- infinite sequence: domain is infinite

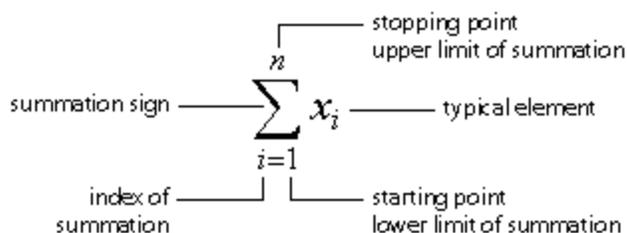
**Sequence/Calculator:** 1) Set [MODE] to SEQ  
2) [Y=] and enter formula (use the [X,T,Θ,n] button for variables)  
3) [2<sup>nd</sup>] + [GRAPH] to view (ie, "TABLE" command)

**Recursive Formulas:** Sequences defined by the first term and the  $n^{\text{th}}$  term.

EXAMPLE:  $S_1 = 1$ ,  $S_n = 4 \cdot S_{n-1}$

**Recursive/Calculator:** 1) Set [MODE] to SEQ  
2) [Y=] and enter formula  
(use the [X,T,Θ,n] button for "n")  
(use the "u" [2<sup>nd</sup>]+[7] for S)  
3) Enter 1<sup>st</sup> term below "u" (nMin)  
4) [2<sup>nd</sup>] + [GRAPH] to view (ie, "TABLE" command)

**Summation Notation:** Finds the sum of the first "n" terms of a sequence ( $a_1 + a_2 + a_3 + \dots + a_n$ )



**Summation/Calculator:** 1) [2<sup>nd</sup>] + [STAT] → MATH → 5:Sum(  
2) [2<sup>nd</sup>] + [STAT] → OPS → 5:Seq(  
3) Expr: 6X+8  
Variable: X  
Start: 1  
End: 10  
Step: 1  
Paste: → [ENTER] + [ENTER]

## 11-2 Arithmetic Sequences *(on formula chart)*

**Explicit:**       $a_n = a_1 + d(n-1)$   
                     $a_1$  = first term  
                     $d$  = common difference (any number minus the number before it)  
                     $n$  = index (integer location of number in the sequence)

**Recursive:**       $a_1 = [\text{some number}]; \quad a_n = a_{n-1} + d$

**Arithmetic Series:** The sum of an arithmetic sequence

$$S_n = \frac{n}{2} (a_1 + a_n)$$

## 11-3 Geometric Sequences and Series *(on formula chart)*

**Explicit:**       $a_n = a_1 \cdot r^{n-1}$   
                     $a_1$  = first term  
                     $r$  = common ratio (any number divided by the number before it)  
                     $n$  = index (integer location of number in the sequence)

**Recursive:**       $a_1 = [\text{some number}]; \quad a_n = a_{n-1} \cdot r$

**Finite Geometric Series:** The sum of a finite geometric sequence

$$S_n = a_1 \cdot \left( \frac{1 - r^n}{1 - r} \right) \quad \text{where } |r| > 1$$

**Infinite Geometric Series:** The sum of an infinite geometric sequence

$$S_n = \frac{a_1}{1 - r} \quad \text{where } |r| < 1$$